

## Biostat Exam 2, F00 (Key)

Covers probability models, intro to confidence intervals, intro to significance testing, one-sample  $t$  statistics, and paired sample  $t$  statistics. Time limit: 1.25 hours.

### Short Answer

- Suppose we take a simple random sample from a population in which  $N = 125$ . Population members are identified with numbers 1 through 125. What is the probability that a given person is selected at random?  
 $1 / 125$ \_\_\_\_\_
- A knowledgeable doctor says that your chances of surviving a particularly virulent illness is 50:50. This probability is conceived on:
  - logic
  - experience
  - subjectivity
  - none of the above
- The binomial distribution is characterized by two parameters. Name these (or list their symbols, your choice):  
 $n$  (no. of trials) \_\_\_\_\_  
 $p$  (probability of success) \_\_\_\_\_
- Normal distributions are characterized by two parameters. Name these:  
 $\mu$  (mean) \_\_\_\_\_  
(standard deviation) \_\_\_\_\_
- $t$  distributions are characterized by one parameter. Name this parameter.  
 $df$  \_\_\_\_\_
- Approximately what percentage of normally distributed values will fall within  $\pm 2$  standard deviations of  $\mu$ ?  
95% \_\_\_\_\_
- Any single mean must be viewed as an example of similar means from a population of experiments done under the same conditions. These hypothetical means would form a:
  - standard error of the mean
  - standard deviation
  - \*\*sampling distribution of means
  - confidence interval
- The theorem that states SDMs tend toward normality is the:
  - \*\*central limit theorem
  - law of large numbers
  - law of unbiasedness
  - standard error of the mean
- A 95% confidence interval for a mean has a 95% chance of capturing:
  - $\bar{x}$
  - \*\* $\mu$
  - 
  - $sem$
- The *probability* of falsely rejecting  $H_0$  is:
  - 
  - 
  - confidence
  - power

11. Which test is used when testing a mean when  $\sigma$  is known?
- \*\*one-sample  $z$  test
  - one-sample  $t$  test
  - paired  $t$  test
  - none of the above
12. An investigator is looking for a mean difference greater than 0. Select the correct alternative hypothesis.
- $H_1: \mu < 0$
  - \*\* $H_1: \mu > 0$
  - $H_1: \mu = 0$
  - $H_1: \mu \neq 0$
13. Inference is generalizing from a \_\_\_\_\_ to a \_\_\_\_\_ with \_\_\_\_\_ calculated degree of certainty.
- population . . . sample
  - \*\*sample . . . population
  - statistic . . . estimator
  - estimator . . . statistic
14. A  $p$  value is greater than .1 suggests data are:
- \*\*not significant
  - marginally significant
  - significant
  - highly significant
15. A jury acquits a man who did the crime he is accused of. This is analogous to a:
- type I error
  - \*\*type II error
  - $p$  value
  - alpha
16. Power is the probability of :
- a type I error
  - a type II error
  - avoidance of a type I error
  - \*\*avoidance of a type II error
17.  $t$  distributions with few degrees of freedom are \_\_\_\_\_ than standard normal distributions.
- \*\*flatter
  - more peaked
  - similar to
  - none of the above
18.  $t$  distributions with infinite degrees of freedom are \_\_\_\_\_ than standard normal distributions.
- flatter
  - more peaked
  - the same as
  - none of the above
19. The analysis of paired differences is similar to the analysis of a single sample except that it is directed toward:
- alpha
  - beta
  - gamma
  - \*\*delta
20. What percentage of 95% confidence intervals will fail to capture the parameter?

## Calculations

1.  $X$  is a binomial random variable with  $n = 10$  and  $p = .15$ . What is the probability of observing exactly 1 success in a sample? Show all work. (Use the back of the page if you run out of room.) [4 pts]

$$\Pr(X = 1) = {}_{10}C_1(.15^1)(.85^9) = (10)(.15)(.2316) = .3474$$

2.  $z_{.8413} = +1$  \_\_\_\_\_

3.  $z_{.1587} = -1$  \_\_\_\_\_

4. In a sample of  $n = 25$ ,  $\bar{x} = 126$ , and  $s = 40$ . Calculate a 95% confidence interval for  $\mu$ . Show all work. [6 pts]

$$126 \pm (t_{24,.975})(40/\text{sqrt}(25)) = 126 \pm (2.06)(8) = 126 \pm 16.48 = (109.52, 142.48)$$

5. Testosterone levels (Int. Units) are taken before and after watching a football game. Data are:

<u>Before</u>	<u>After</u>
83	81
96	92
88	88
99	93

Test the data to see if there has been a significant change in testosterone levels. Show all testing steps. Draw the  $p$  value regions on the curve.

$$H_0: \mu_d = 0 \quad H_1: \mu_d \text{ not } = 0$$

$$x_d = 12$$

$$\text{mean} = 12 / 4 = 3$$

$$SS_d = 20$$

$$s_d = \text{sqrt}(20/3) = 2.582$$

$$t_{\text{stat}} = (3 - 0) / (2.582 / \text{sqrt}(4)) = 2.32$$

$$df = 4 - 1 = 3$$

Curve not drawn in this document, but should show two tails shaded and at  $+2.32$  and  $-2.32$  with each tail representing half of the  $p$ -value and  $.1 < p < .2$ . The test is not significant.

